## Victor Donnay

# Special surfaces discussed in my article <br> "Chaotic Geodesic Motion: An extension of M.C. Escher's Circle Limit Designs" 

One-minute movie: "Turning a Rectangle into a Torus"

Five-minute movie on the Costa surface

# Schwarz P-Surface 

A minimal surface discovered by
H. A. Schwarz in 1890.


## Sphere with Chaotic Geodesic Motion

Taking the Schwarz P-surface and attaching focusing caps to the ends of the Schwarz P-surface produces a sphere. The geodesic motion on this sphere is chaotic.


# Four copies of the Schwarz surface joined together 



# Torus with Chaotic Geodesic Motion 

Taking the surface formed by four copies of the Schwarz P-surface and attaching focusing caps to the ends produces a torus. The geodesic motion on this torus is chaotic.



# Torus with 2 Holes 

Two-holed torus formed by connecting the edges of an eight-sided fundamental region, decorated with Escher's fish pattern.

Sculpture and photograph by Douglas Dunham.
$60$

## Torus Movie

A one minute sound movie showing how a torus (doughnut) can be made by connecting opposite edges of a rectangle.

## Turning a Rectangle into a Torus



Click on the rectangle to view the movie

## Costa Movie

A 5-minute sound movie showing the geometry and topology of the Costa Minimal Surface. The Costa surface is a strangely shaped doughnut. The video shows the connection between the Costa doughnut and the standard doughnut.

## The Geometry and Topology of the Costa Surface



Click on the rectangle to view the movie

