Figure 3 shows a simple simulation with RED gateways. The network is shown in Figure 4. The simulation contains four FTP connections, each with a maximum window roughly equal to the delay-bandwidth product, which ranges from 33 to 112 packets. The RED gateway parameters are set as follows:  $w_q =$ 0.002,  $min_{th} = 5$  packets,  $max_{th} = 15$  packets, and  $max_p = 1/50$ . The buffer size is sufficiently large that packets are never dropped at the gateway due to buffer overflow; in this simulation the RED gateway controls the average queue size, and the actual queue size never exceeds forty packets.



Figure 4: Simulation network.

For the charts in Figure 3, the x-axis shows the time in seconds. The bottom chart shows the packets from nodes 1-4. Each of the four main rows shows the packets from one of the four connections; the bottom row shows node 1 packets, and the top row shows node 4 packets. There is a mark for each data packet as it arrives at the gateway and as it departs from the gateway; at this time scale, the two marks are often indistinguishable. The y-axis is a function of the packet sequence number; for packet number nfrom node *i*, the y-axis shows  $n \mod 90 + (i-1)100$ . Thus, each vertical 'line' represents 90 consecutivelynumbered packets from one connection arriving at the gateway. Each 'X' shows a packet dropped by the gateway, and each 'X' is followed by a mark showing the retransmitted packet. Node 1 starts sending packets at time 0, node 2 starts after 0.2 seconds, node 3 starts after 0.4 seconds, and node 4 starts after 0.6 seconds.

The top chart of Figure 3 shows the instantaneous queue size q and the calculated average queue size avg. The dotted lines show  $min_{th}$  and  $max_{th}$ , the minimum and maximum thresholds for the average queue size. Note that the calculated average queue size avg changes fairly slowly compared to q. The

bottom row of X's on the bottom chart shows again the time of each dropped packet.

This simulation shows the success of the RED gateway in controlling the average queue size at the gateway in response to a dynamically changing load. As the number of connections increases, the frequency with which the gateway drops packets also increases. There is no global synchronization. The higher throughput for the connections with shorter roundtrip times is due to the bias of TCP's window increase algorithm in favor of connections with shorter roundtrip times (as discussed in [6, 7]). For the simulation in Figure 3 the average link utilization is 76%. For the following second of the simulation, when all four sources are active, the average link utilization is 82%. (This is not shown in Figure 3.)



Figure 5: Comparing Drop Tail and RED gateways.



Figure 6: Simulation network.

Because RED gateways can control the average queue size while accommodating transient congestion, RED gateways are well-suited to provide high throughput and low *average* delay in high-speed networks with TCP connections that have large windows. The RED gateway can accommodate the short burst in the queue required by TCP's slowstart phase; thus RED gateways control the *average* queue size while still allowing TCP connections to smoothly open their windows. Figure 5 shows the results of simulations of the network in Figure 6 with two TCP connections, each with a maximum window of 240 packets, roughly equal to the delay-bandwidth product. The two connections are started at slightly different times. The simulations compare the performance of Drop Tail and of RED gateways.

In Figure 5 the x-axis shows the total throughput as a fraction of the maximum possible throughput on the congested link. The y-axis shows the average queue size in packets (as seen by arriving packets). Five 5-second simulations were run for each of 11 sets of parameters for Drop Tail gateways, and for 11 sets of parameters for RED gateways; each mark in Figure 5 shows the results of one of these five-second simulations. The simulations with Drop Tail gateways were run with the buffer size ranging from 15 to 140 packets; as the buffer size is increased, the throughput and the average queue size increase correspondingly. In order to avoid phase effects in the simulations with Drop Tail gateways, the source node takes a random time drawn from the uniform distribution on [0, t]seconds to prepare an FTP packet for transmission, where t is the bottleneck service time of 0.17 ms. [7].

The simulations with RED gateways were all run with a buffer size of 100 packets, with  $min_{th}$  ranging from 3 to 50 packets. For the RED gateways,  $max_{th}$ is set to  $3 \min_{th}$ , with  $w_a = 0.002$  and  $\max_{th} = 1/50$ . The dashed lines show the average delay (as a function of throughput) approximated by 1.73/(1-x)for the simulations with RED gateways, and approximated by  $0.1/(1-x)^3$  for the simulations with Drop Tail gateways. For this simple network with TCP connections with large windows, the network power (the ratio of throughput to delay) is higher with RED gateways than with Drop Tail gateways. There are several reasons for this difference. With Drop Tail gateways with a small maximum queue, the queue drops packets while the TCP connection is in the slow-start phase of rapidly increasing its window, reducing throughput. On the other hand, with Drop Tail gateways with a large maximum queue the average delay is unacceptably large. In addition, Drop Tail gateways are more likely to drop packets from both connections at the same time, resulting in global synchronization and a further loss of throughput.

Later in the paper, we discuss simulation results from networks with a more diverse range of connections. The RED gateway is not specifically designed for a network dominated by bulk data transfer; this is simply an easy way to simulate increasingly-heavy congestion at a gateway.

# 6 Calculating the average queue length

The RED gateway uses a low-pass filter to calculate the average queue size. Thus, the short-term increases in the queue size that result from bursty traffic or from transient congestion do not result in a significant increase in the average queue size.

The low-pass filter is an exponential weighted moving average (EWMA):

$$avg \leftarrow (1 - w_q)avg + w_q q.$$
 (1)

The weight  $w_q$  determines the time constant of the low-pass filter. The following sections discuss upper and lower bounds for setting  $w_q$ . The calculation of the average queue size can be implemented particularly efficiently when  $w_q$  is a (negative) power of two, as shown in Section 11.

#### 6.1 An upper bound for $w_q$

If  $w_q$  is too large, then the averaging procedure will not filter out transient congestion at the gateway.

Assume that the queue is initially empty, with an average queue size of zero, and then the queue increases from 0 to L packets over L packet arrivals. After the Lth packet arrives at the gateway, the average queue size  $avg_L$  is

$$avg_{L} = \sum_{i=1}^{L} i w_{q} (1 - w_{q})^{L-i}$$
  
$$= w_{q} (1 - w_{q})^{L} \sum_{i=1}^{L} i (\frac{1}{1 - w_{q}})^{i}$$
  
$$= L + 1 + \frac{(1 - w_{q})^{L+1} - 1}{w_{q}}.$$
 (2)

This derivation uses the following identity [9, p. 65]:

$$\sum_{i=1}^{L} ix^{i} = \frac{x + (Lx - L - 1)x^{L+1}}{(1-x)^{2}}.$$

Figure 7 shows the average queue size  $avg_L$  for a range of values for  $w_q$  and L. The x-axis shows  $w_q$  from 0.001 to 0.005, and the y-axis shows L from 10 to 100. For example, for  $w_q = 0.001$ , after a queue increase from 0 to 100 packets, the average queue size  $avg_{100}$  is 4.88 packets.

Given a minimum threshold  $min_{th}$ , and given that we wish to allow bursts of L packets arriving at the gateway, then  $w_q$  should be chosen to satisfy the following equation for  $avg_L < min_{th}$ :

$$L + 1 + \frac{(1 - w_q)^{L+1} - 1}{w_q} < min_{th}.$$
 (3)



Figure 7:  $avg_L$  as a function of  $w_q$  and L.

Given  $min_{th} = 5$ , and L = 50, for example, it is necessary to choose  $w_q \leq 0.0042$ .

#### 6.2 A lower bound for $w_q$

RED gateways are designed to keep the calculated average queue size avg below a certain threshold. However, this serves little purpose if the calculated average avg is not a reasonable reflection of the current average queue size. If  $w_q$  is set too low, then avg responds too slowly to changes in the actual queue size. In this case, the gateway is unable to detect the initial stages of congestion.

Assume that the queue changes from empty to one packet, and that, as packets arrive and depart at the same rate, the queue remains at one packet. Further assume that initially the average queue size was zero. In this case it takes  $-1/\ln(1 - w_q)$  packet arrivals (with the queue size remaining at one) until the average queue size avg reachs 0.63 = 1 - 1/e [35]. For  $w_q = 0.001$ , this takes 1000 packet arrivals; for  $w_q = 0.002$ , this takes 500 packet arrivals; for  $w_q = 0.003$ , this takes 333 packet arrivals. In most of our simulations we use  $w_q = 0.002$ .

#### 6.3 Setting $min_{th}$ and $max_{th}$

The optimal values for  $min_{th}$  and  $max_{th}$  depend on the desired average queue size. If the typical traffic is fairly bursty, then  $min_{th}$  must be correspondingly large to allow the link utilization to be maintained at an acceptably high level. For the typical traffic in our simulations, for connections with reasonably large delay-bandwidth products, a minimum threshold of one packet would result in unacceptably low link utilization. The discussion of the optimal average queue size for a particular traffic mix is left as a question for future research. The optimal value for  $max_{th}$  depends in part on the maximum average delay that can be allowed by the gateway.

The RED gateway functions most effectively when  $max_{th} - min_{th}$  is larger than the typical increase in the calculated average queue size in one roundtrip time. A useful rule-of-thumb is to set  $max_{th}$  to at least twice  $min_{th}$ .

## 7 Calculating the packet-marking probability

The initial packet-marking probability  $p_b$  is calculated as a linear function of the average queue size. In this section we compare two methods for calculating the final packet-marking probability, and demonstrate the advantages of the second method. In the first method, when the average queue size is constant the number of arriving packets between marked packets is a geometric random variable; in the second method the number of arriving packets between marked packets is a uniform random variable.

The initial packet-marking probability is computed as follows:

$$p_b \leftarrow max_p(avg - min_{th})/(max_{th} - min_{th}).$$

The parameter  $max_p$  gives the maximum value for the packet-marking probability  $p_b$ , achieved when the average queue size reaches the maximum threshold.

Method 1: Geometric random variables. In Method 1, let each packet be marked with probability  $p_b$ . Let the intermarking time X be the number of packets that arrive, after a marked packet, until the next packet is marked. Because each packet is marked with probability  $p_b$ ,

$$Prob[X = n] = (1 - p_b)^{n-1} p_b.$$

Thus with Method 1, X is a geometric random variable with parameter  $p_b$ , and  $E[X] = 1/p_b$ .

With a constant average queue size, the goal is to mark packets at fairly regular intervals. It is undesirable to have too many marked packets close together, and it is also undesirable to have too long an interval between marked packets. Both of these events can result in global synchronization, with several connections reducing their windows at the same time, and both of these events can occur when X is a geometric random variable.  $\Box$ 

Method 2: Uniform random variables. A more desirable alternative is for X to be a *uniform* random variable from  $\{1, 2, ..., 1/p_b\}$  (assuming for simplicity that  $1/p_b$  is an integer). This is achieved



Figure 8: Randomly-marked packets, comparing two packet-marking methods.

if the marking probability for each arriving packet is  $p_b/(1 - count \cdot p_b)$ , where *count* is the number of unmarked packets that have arrived since the last marked packet. Call this Method 2. In this case,

$$Prob[X = n] = \frac{p_b}{1 - (n - 1)p_b} \prod_{i=0}^{n-2} \left( 1 - \frac{p_b}{1 - i p_b} \right)$$
$$= p_b \text{ for } 1 \le n \le 1/p_b,$$

and

$$Prob[X = n] = 0 \text{ for } n > 1/p_b.$$

For Method 2,  $E[X] = 1/(2p_b) + 1/2$ .  $\Box$ 

Figure 8 shows an experiment comparing the two methods for marking packets. The top line shows Method 1, where each packet is marked with probability p, for p = 0.02. The bottom line shows Method 2, where each packet is marked with probability p/(1+ip), for p = 0.01, and for i the number of unmarked packets since the last marked packet. Both methods marked roughly 100 out of the 5000 arriving packets. The x-axis shows the packet number. For each method, there is a dot for each marked packet. As expected, the marked packets are more clustered with Method 1 than with Method 2.

For the simulations in this paper, we set  $max_p$  to 1/50. When the average queue size is halfway between  $min_{th}$  and  $max_{th}$ , the gateway drops, on the average, roughly one out of 50 (or one out of  $1/max_n$ ) of the arriving packets. RED gateways perform best when the packet-marking probability changes fairly slowly as the average queue size changes; this helps to discourage oscillations in the average queue size and in the packet-marking probability. There should never be a reason to set  $max_p$  greater than 0.1, for example. When  $max_p = 0.1$ , then the RED gateway marks close to 1/5th of the arriving packets when the average queue size is close to the maximum threshold (using Method 2 to calculate the packet-marking probability). If congestion is sufficiently heavy that the average queue size cannot be controlled by marking close to 1/5th of the arriving packets, then after

the average queue size exceeds the maximum threshold, the gateway will mark every arriving packet.

### 8 Evaluation of RED gateways

In addition to the design goals discussed in Section 3, several general goals have been outlined for congestion avoidance schemes [14, 16]. In this section we describe how our goals have been met by RED gateways.

• Congestion avoidance. If the RED gateway in fact drops packets arriving at the gateway when the average queue size reaches the maximum threshold, then the RED gateway guarantees that the calculated average queue size does not exceed the maximum threshold. If the weight  $w_q$  for the EWMA procedure has been set appropriately [see Section 6.2], then the RED gateway in fact controls the actual average queue size. If the RED gateway sets a bit in packet headers when the average queue size exceeds the maximum threshold, rather than dropping packets, then the RED gateway relies on the cooperation of the sources to control the average queue size.

• Appropriate time scales. After notifying a connection of congestion by marking a packet, it takes at least a roundtrip time for the gateway to see a reduction in the arrival rate. In RED gateways the time scale for the detection of congestion roughly matches the time scale required for connections to respond to congestion. RED gateways don't notify connections to reduce their windows as a result of transient congestion at the gateway.

• No global synchronization. The rate at which RED gateways mark packets depends on the level of congestion. During low congestion, the gateway has a low probability of marking each arriving packet, and as congestion increases, the probability of marking each packet increases. RED gateways avoid global synchronization by marking packets at as low a rate as possible.

• Simplicity. The RED gateway algorithm could

be implemented with moderate overhead in current networks, as discussed further in Section 11.

• Maximizing global power<sup>4</sup>. The RED gateway explicitly controls the average queue size. Figure 5 shows that for simulations with high link utilization, global power is higher with RED gateways than with Drop Tail gateways. Future research is needed to determine the optimum average queue size for different network and traffic conditions.

• Fairness. One goal for a congestion avoidance mechanism is fairness. This goal of fairness is not well-defined, so we simply describe the performance of the RED gateway in this regard. The RED gateway does not discriminate against particular connections or classes of connections. (This is in contrast to Drop Tail or Random Drop gateways, as described in [7]). For the RED gateway, the fraction of marked packets for each connection is roughly proportional to that connection's share of the bandwidth. However, RED gateways do not attempt to ensure that each connection receives the same fraction of the total throughput, and do not explicitly control misbehaving users. RED gateways provide a mechanism to identify the level of congestion, and RED gateways could also be used to identify connections using a large share of the total bandwidth. If desired, additional mechanisms could be added to RED gateways to control the throughput of such connections during periods of congestion.

• Appropriate for a wide range of environments. The randomized mechanism for marking packets is appropriate for networks with connections with a range of roundtrip times and throughput, and for a large range in the number of active connections at one time. Changes in the load are detected through changes in the average queue size, and the rate at which packets are marked is adjusted correspondingly. The RED gateway's performance is discussed further in the following section.

Even in a network where RED gateways signals congestion by dropping marked packets, there are many occasions in a TCP/IP network when a dropped packet does not result in any decrease in load at the gateway. If the gateway drops a data packet for a TCP connection, this packet drop will be detected by the source, possibly after a retransmission timer expires. If the gateway drops an ACK packet for a TCP connection, or a packet from a non-TCP connection, this packet drop could go unnoticed by the source. However, even for a congested network with a traffic mix dominated by short TCP connections or by non-TCP connections, the RED gateway

 ${}^4Power$  is defined as the ratio of throughput to delay.

still controls the average queue size by dropping all arriving packets when the average queue size exceeds a maximum threshold.

#### 8.1 Parameter sensitivity

This section discusses the parameter sensitivity of RED gateways. Unlike Drop Tail gateways, where the only free parameter is the buffer size, RED gateways have additional parameters that determine the upper bound on the average queue size, the time interval over which the average queue size is computed, and the maximum rate for marking packets. The congestion avoidance mechanism should have low parameter sensitivity, and the parameters should be applicable to networks with widely varying bandwidths.

The RED gateway parameters  $w_q$ ,  $min_{th}$ , and  $max_{th}$  are necessary so that the network designer can make conscious decisions about the desired average queue size, and about the size and duration in queue bursts to be allowed at the gateway. The parameter  $max_p$  can be chosen from a fairly wide range, because it is only an upper bound on the actual marking probability  $p_b$ . If congestion is sufficiently heavy that the gateway cannot control the average queue size by marking at most a fraction  $max_p$  of the packets, then the average queue size will exceed the maximum threshold, and the gateway will mark every packet until congestion is controlled.

We give a few rules that give adequate performance of the RED gateway under a wide range of traffic conditions and gateway parameters.

1: Ensure adequate calculation of the average queue size: set  $w_q \ge 0.001$ . The average queue size at the gateway is limited by  $max_{th}$ , as long as the calculated average queue size avg is a fairly accurate reflection of the actual average queue size. The weight  $w_q$  should not be set too low, so that the calculated average queue length does not delay too long in reflecting increases in the actual queue length [See Section 6]. Equation 3 describes the upper bound on  $w_q$  required to allow the queue to accommodate bursts of L packets without marking packets.

2: Set  $min_{th}$  sufficiently high to maximize network power. The thresholds  $min_{th}$  and  $max_{th}$ should be set sufficiently high to maximize network power. As we stated earlier, more research is needed on determining the optimal average queue size for various network conditions. Because network traffic is often bursty, the actual queue size can also be quite bursty; if the average queue size is kept too low, then the output link will be underutilized.

3: Make  $max_{th} - min_{th}$  sufficiently large to avoid global synchronization. Make  $max_{th}$  -  $min_{th}$  larger than the typical increase in the average queue size during a roundtrip time, to avoid the global synchronization that results when the gateway marks many packets at one time. One rule of thumb would be to set  $max_{th}$  to at least twice  $min_{th}$ . If  $max_{th} - min_{th}$  is too small, then the computed average queue size can regularly oscillate up to  $max_{th}$ ; this behavior is similar to the oscillations of the queue up to the maximum queue size with Drop Tail gateways.