

Reversing f0dder's CrackMe #2

by Cardenal Mendoza

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1 Introduction

This essay is not for absolute beginners, although reversing the crackme is not very hard, but coding a keygen is. Heh, coding a 90% keygen is hard, but i guess coding a 100% keygen is impossible because you could only brutforce the last part of the crackme :(Apart from that it is a very nice crackme, but decide by yourself...

2 Tools used

1. SoftIce 4.05 for NT (I use Win 2000 for cracking)
2. Win32dasm (I guess IDA would be better - but I don't have it)
3. Ultraedit
4. f0dder's crackme #2 (of course ;)
5. some imagination or a great mathematical knowledge (for coding the keygen)

3 Reversing the crackme

First start the crackme and look what intresting stuff you can find. Well, since there is only one box to enter something, do that and press the bitmap. A nice message pops up telling you that the door is still locked. You stupid idiot, didn't you set a breakpoint on *GetWindowTextA* and *GetDlgItemTextA* first? Ok, put those breakpoints and click again... Again the message pops up, well, some smart people would now set a breakpoint on *hmemcpy*, but remember, I crack under Win 2000, there is no *hmemcpy*, so we must use another way. Again many people would say now, that we could use *memcpy*, but *memcpy* is not the same as *hmemcpy*, for cracking purposes *memcpy* is useless, trust me.

Well, I got some background information from f0dder on irc :) He said I should use the dead listing, at least he said this for #1, but I hope it will help us here, too. Just disassemble it in your preferred disassembler, I will use Win32dasm

since I don't have IDA. Anyway, if you did this, just trace a little bit through the code. Better print it completely (I hope you have a nice printer ;). First look at the imports. This are the two most important ones:

1. CreateFileA
2. GetDlgItemTextA

So what do this two imports tell us?

1. Its a keyfile protection (We should have read the readme.txt *g*)
2. It probably uses GetDlgItemTextA for getting the user input. (Hmm, ' we check this?)

I must admit that we could get the first information from the readme.txt, too, but who reads such txts? The second one is more interesting, how can it use GetDlgItemTextA without breaking on it? Perhaps f0dder thinks he is smart and only checks for the serial if a valid keyfile is found.

Now lets jump to programs entry point:

```
//*****Program Entry Point*****  
:004013F3      push 00000000  
:004013F8      call dword ptr[00402014]  
:004012FE      mov  dword ptr[0040334C], eax  
:00401403      xor  ebx, ebx  
:00401405      xor  eax, eax  
:00401407      push eax  
:00401408      push 00401320  
:0040140D      push ebx  
:0040140E      push 00000065  
:00401413      push eax  
:00401414      call dword ptr[0040202C]  
:0040141A      push eax  
:0040141B      call dword ptr[00402004]  
:00401421      ret
```

What does us that part of the code tell? You should know this by yourself, if not, read iczelions win32asm tutorials. This is just the start of every Win32 dialog based application. Beside that it tells us nothing usefull, but it is always better to check, because the coder could check for the keyfile even before the call to *DialogBoxParamA*. Now lets scroll up again until we see the start of the code:

```
*****ASSEMBLY CODE LISTING*****  
//*****Start of Code in Object .text*****  
Program Entry Point=004013F3
```

```

:00401000    mov     edi, 004030A7
:00401005    mov     cl, 03
:00401007    dec     byte ptr[edi]
:00401009    dec     byte ptr[edi+01]
:0040100C    dec     byte ptr[edi+02]
:0040100F    dec     byte ptr[edi+03]
:00401012    add     edi, 00000004
:00401015    dec     cl
:00401017    jne     00401007

```

This part is also easy to understand. We see that 004030A7 is a string reference to 'tlmfupo/lfz'. try to analyze it before you read on, its not that hard if you understand assembly. All it does is decreasing each byte in the string by one, lets do it on a paper, too. Yes, the result is 'skeleton.key'. This looks like the name of our keyfile. After this code, the location 004012C0 is called, lets take a look at it:

```

:004012C0    push    00000000
:004012C5    push    00000000
:004012CA    push    00000003
:004012CF    push    00000000
:004012D4    push    00000000
:004012D9    push    80000000
:004012DE    push    eax
:004012DF    call    dword ptr[0040200C]
:004012E5    cmp     eax, FFFFFFFF
:004012EA    jne     004012EE
:004012EC    xor     eax, eax
:004012EE    ret

```

As expected this code snippet does nothing more than opening the keyfile. If it is succesfully, it returns, if not, it sets eax=0 before returning. After returning the eip will be 00401021. I won't list every small piece of code, as I said you should print it by yourself. After returning, the program checks if the file is present (00401021), if not it jumps to 0040104C. Now trace into the following calls and see what happens there. I assume not to use SoftIce, yet, in order to see how useful a dead listing can be. Lets analyze the code, the call at 00401034 does nothing more than reading the whole file into memory and the call at 00401045 closes the file again. Notice the cmps/jmps after these two calls, if one of them fails, it jumps to 0040104C, setting a flag that the keyfile is not found. This is the reason we couldn't break on *GetDlgItemTextA* If you examine the call at 004012F7 you will notice that it reads 256 bytes, so our keyfile must be at least 256 bytes long. After those we could append something like "Keyfile generated by Cardenal Mendoza", but this is not an expensive app and I don't care if somebody steals a keygen for a crackme :P

Lets go reversing again. Write down the address of the keyfile in memory. Now

search through the dead listig for this address... ahh we are lucky, it occurs only two times, for the first time when the file is read into memory, for the second time at 00401134. The second location seems quite intresting. We should take a closer look at it:

```
:00401134      mov     esi, 004030B4
:00401139      mov     edi, 004031B4
:0040113E      xor     ecx, ecx
:00401140      mov     cl, 80
:00401142      mov     al, byte ptr[esi]
:00401144      cmp     al, 30
:00401146      jb      004012A8
:0040114C      cmp     al, 39
:0040114E      ja      00401158
:00401154      sub     al, 30
:00401156      jmp     0040116A
:00401158      cmp     al, 41
:0040115A      jb      004012A8
:00401160      cmp     al, 46
:00401162      ja      004012A8
:00401168      sub     al, 37
:0040116A      mov     ah, al
:0040116C      shl     ah, 04
:0040116F      mov     al, byte ptr[esi+01]
:00401172      cmp     al, 30
:00401174      jb      004012A8
:0040117A      cmp     al, 39
:0040117C      ja      00401186
:00401182      sub     al, 30
:00401184      jmp     00401198
:00401186      cmp     al, 41
:00401188      jb      004012A8
:0040118E      cmp     al, 46
:00401190      ja      004012A8
:00401196      sub     al, 37
:00401198      or      ah, al
:0040119A      mov     byte ptr[edi], ah
:0040119C      inc     esi
:0040119D      inc     esi
:0040119E      inc     edi
:0040119F      dec     cl
:004011A1      jne     00401142
:004011A3      ret
```

I suggest that either you have a good knowledge of that shift and logical operations or you simply look in SoftIce what happens. I did the second one because

I hate stuff like `or` and `shl`. I make it short, the keyfile is only valid, if it has only characters between '0' and '9' and 'A' and 'F'. Think about this, that are all possible characters for hexadecimal numbers. If you analyze the code after the check you will know why. Just look what happens:

Keyfile:	A	2	D	1	F	9	E	1	7	F
Array:	A2	D1	F9	E1	7F

The code simply converts two ASCII values (for example 'A' and '2') to one byte (A2).

I guess this is clear. How should we go on? Starting to trace with SoftIce? Oh, no, just look at the first part of the code snippet: "Referenced by a Call...". Lets look where the code part is called from. There you should see 5 calls. In my opinion tgis looks like a protection =) I think we should look into the next call. Hehe, a reference to *GetDlgItemTextA*, now we know that we are right.

```

:004011A4      push 00000011
:004011A9      push 00403334
:004011AE      push 000003E8
:004011B3      push dword ptr[00403350]
:004011B9      call dword ptr[00402024]
:004011BF      cmp  eax, 00000010
:004011C4      ja   004012A8
:004011CA      je   004011E8
:004011CC      mov  esi, 00403334
:004011D1      mov  edi, 00403334
:004011D6      add  edi, eax
:004011D8      sub  eax, 00000010
:004011DD      neg  eax
:004011DF      mov  dl, byte ptr[esi]
:004011E1      mov  byte ptr[edi], dl
:004011E3      inc  esi
:004011E4      inc  edi
:004011E5      dec  eax
:004011E6      jne  004011DF
:004011E8      mov  esi, 00403334
:004011ED      mov  edi, 00403234
:004011F2      mov  ecx, 00000004
:004011F7      repz
:004011F8      movsd
:004011F9      mov  ecx, 00000070
:004011FE      mov  esi, 00403234
:00401203      mov  al, byte ptr[esi]
:00401205      xor  al, byte ptr[esi+01]
:00401208      mov  byte ptr[edi], al
:0040120A      inc  esi

```

```

:0040120B      inc     esi
:0040120C      dec     ecx
:0040120D      jne     00401203
:0040120F      ret

```

Slowly the dead listing begins to bore me, so let's make it fast ;)

As you can see, this part does nothing more than getting our serial, then checking if it is lower than 16 in length, and if yes, it appends the serial from the beginning until the serial is 16 characters long. Any serial which is longer is invalid. This is easy to see out of the dead listing. If not you should learn assembler. I won't explain all instructions, because I said this is not for the very beginner. If the serial is 16 byte long, it is xored in a special way. It xors the first and the second array element and writes the result into the 17th, then it xors the 3rd and the 4th to the 18th and so on. This is done until the serial-array is 128 bytes long. Now look into the next call, as you can easily see, it does nothing more than just xoring those two arrays, which are both 128 bytes long. I think this is even for newbies easy to understand.

Ok, the next call is a important one, so let's take a deeper look at it:

```

:00401234      mov     esi, 004032B4
:00401239      mov     ecx, 00000080
:0040123E      mov     eax, dword ptr[0040309A]
:00401243      xor     al, byte ptr[esi]
:00401245      rol     eax, 1
:00401247      inc     esi
:00401248      dec     ecx
:00401249      jne     00401243
:0040124B      cmp     eax, dword ptr[0040309E]
:00401251      jne     004012B4
:00401253      ret

```

Well, I got heavy headaches because of this call when I coded a keygen for the crackme. The code itself should be clear. first eax is set to 0BADC0DEh and then it xors al with each byte of the array and rolls eax after every xor. Then after doing the whole loop eax is compared to the dword in 0040309E. Look in SoftIce to look what's in it. Yes, it is 0FCC5A375h. Hmm, that are all simply instructions. But now think how to reverse it. Of course it is easy to get a right start or ending value with a good array, but how to get the array with just two values? Well, figure out by yourself, you can always look at my keygen in appendix A. My keygen is very crappy and if I am honest, I now don't know why it works, erm, I know the principle but it was a lot of try&error testing until I got it working. In appendix B there is a mail by +spath about a mathematical way to solve it, but I must admit that I am not so good in mathematics and I don't understand too much of it.

Code a keygen by yourself, you will see that it is senseless:(

If you analyze the next call you will see why. Did you notice that strange looking code at 00401064 before? We jump to it after the last call, which does nothing

more than xoring the code with our array. This means that we can't make a good keygen, we have to brute force a valid array first. But that is not my task, in my opinion a crackme must be crackable, bruteforcing is no cracking at all. f0dder should have called this a brute force me or at least write in to the readme that it is only brute force able, hehe, I didn't read it anyway ;) f0dder says that he wanted to show with this crackme that it is possible to code a protection which is not easily to crack. Sure, this is possible, but i knew it before. But apart from this last part cracking the crackme was fun.

4 Conclusions

So what did we learn from this crackme? I don't know what you learned, but I learned that dead listings can be very useful, at least if the protection is coded in assembly. Ok, I sometimes used SoftIce, for example when the keyfile is converted to the array. Decide by yourself what you learned from it. Always remember, this is my 3rd tutorial and my English is very bad :P If you have any questions mail me at Cardenal@gmx.net.

Please visit these webpages:

1. <http://mendoza.tsx.org> < my webpage
2. <http://www.learn2crack.com> < learn2crack
3. <http://codex.cjb.net> < the codex

5 Appendix I - My keygen source

```
; keymaker.asm
; I know this code is very crappy, but hey, it is only a keygen
; I hope you understand that I don't optimize it if it works ;)
; coded by Cardenal Mendoza [01/29/2000]
; compiles/runs without problems under Win 2000 and Masm
.386
.model flat, stdcall
option casemap:none
; Includes
include \masm32\include\windows.inc
include \masm32\include\kernel32.inc
include \masm32\include\user32.inc
includelib \masm32\lib\kernel32.lib
includelib \masm32\lib\user32.lib
MAINDLG equ 103
ID_EDITNAME equ 1000
ID_EDITSERIAL equ 1001
ID_STATIC equ -1
```

```

KeyGenDlgProc PROTO :DWORD,:DWORD,:DWORD,:DWORD
MakeKey PROTO :DWORD
; The Data Section
.DATA
fmat          db    "%d",0
hInst         dd    0
KeyGenDlg     db    "MAINDLG",0
fname         db    "skeleton.key",0
fhandle       dd    0
xor_array     db    128 dup(0)
ser_array     db    128 dup(0)
fil1array     db    128 dup(0)
fil2array     db    256 dup(0)
bread         dd    0
bwrite        dd    0
; The uninitialized data
.DATA?
szName        db    250 dup(?)
szSerial      db    40  dup(?)
szTmp         db    6   dup(?)
DlgRect       RECT <>
DlgWidth      dd    0
DlgHeight     dd    0
DeskRect      RECT <>
; The code section
.CODE
main:
    invoke    GetModuleHandle, NULL
    mov       hInst, eax
    invoke    DialogBoxParam,hInst, ADDR KeyGenDlg, 0, ADDR KeyGenDlgProc, 0
    invoke    ExitProcess, eax
KeyGenDlgProc PROC hDlg:DWORD, wParam:DWORD, lParam:DWORD
    .IF wParam==WM_INITDIALOG
        push  OFFSET DlgRect
        push  hDlg
        call  GetWindowRect
        call  GetDesktopWindow
        push  OFFSET DeskRect
        push  eax
        call  GetWindowRect
        push  0
        mov   eax, DlgRect.bottom
        sub   eax, DlgRect.top
        mov   DlgHeight, eax
        push  eax
        mov   eax, DlgRect.right
    
```



```

        sub    eax, DlgRect.left
        mov    DlgWidth, eax
        push   eax
        mov    eax, DeskRect.bottom
        sub    eax, DlgHeight
        shr    eax, 1
        push   eax
        mov    eax, DeskRect.right
        sub    eax, DlgWidth
        shr    eax, 1
        push   eax
        push   hDlg
        call   MoveWindow
    .ELSEIF wMsg == WM_DESTROY
        jmp     wmclose
    .ELSEIF wMsg == WM_CLOSE
        jmp     wmclose
    .ELSEIF wMsg == WM_COMMAND
        jmp     wmcommand
    .ENDIF
    xor        eax, eax
    ret
wmclose:
    invoke     EndDialog, hDlg, TRUE
    invoke     ExitProcess, NULL
    ret
wmcommand:
    cmp        word ptr[wParam], IDOK
    jne        notn
    invoke     MakeKey, hDlg
    jmp        rt
notn:
    cmp        wParam, IDOK
    je         wmclose
rt:
    ret
KeyGenDlgProc ENDP
MakeKey PROC USES eax ebx ecx edx esi edi _hDlg:DWORD
    xor        ecx, ecx
    mov        ebx, 666h
    mov        esi, offset xor_array
rnd_lop:
    invoke     GetTickCount
    imul       eax, ebx
    rol        eax, 2
    mov        dword ptr[esi], eax

```

```

    add     esi, 4
    inc     ecx
    rol     ebx, 5
    add     ebx, eax
    cmp     eax, 24
    jl      rnd_lop
    mov     edi, offset xor_array
    mov     ecx, 96
    mov     eax, 0BADCODEh
encr2_lop:
    xor     al, byte ptr[edi]
    rol     eax, 1
    inc     edi
    dec     ecx
    jnz     encr2_lop
    xor     al, 075h
    mov     byte ptr[esi], al
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     edi, offset xor_array
    mov     ecx, 104
    mov     eax, 0BADCODEh
encr1_lop:
    xor     al, byte ptr[edi]
    rol     eax, 1
    inc     edi
    dec     ecx
    jnz     encr1_lop
    xor     al, 0FCh
    mov     byte ptr[esi], al
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi

```

```

mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
rol     eax, 8
xor     al, 0C5h
mov     byte ptr[esi], al
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
rol     eax, 8
xor     al, 0A3h
mov     byte ptr[esi], al
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi
mov     byte ptr[esi], 00
inc     esi

```

```

    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    inc     esi
    mov     byte ptr[esi], 00
    rol     eax, 8
    xor     al, 075h
    mov     byte ptr[esi], al
    inc     esi
    xor     eax, eax
    xor     esi, esi
    xor     edi, edi
    xor     edx, edx
    mov     esi, offset ser_array
    mov     edi, offset xor_array
cp_lop:
    mov     dl, byte ptr[edi]
dada:
    cmp     dl, 48
    jg      dudu
    add     dl, 9
    jmp     dada
dudu:
    cmp     dl, 57
    jl      huhu
    sub     dl, 9
    jmp     dudu
huhu:
    mov     byte ptr[esi], dl
    inc     eax
    inc     edi
    inc     esi
    cmp     eax, 16
    jnz     cp_lop
    mov     edi, offset ser_array
    mov     ecx, 70h
xorma:
    mov     al, byte ptr[edi]
    xor     al, byte ptr[edi+1]
    mov     byte ptr[esi], al
    inc     esi
    inc     edi
    dec     ecx
    jnz     xorma
    xor     eax, eax
    xor     ebx, ebx

```

```

        xor     ecx, ecx
        xor     edx, edx
        xor     esi, esi
        xor     edi, edi
        mov     eax, offset fil1array
        mov     ebx, offset ser_array
        mov     ecx, offset xor_array
        mov     esi, 80h
make_file:
        mov     dl, byte ptr[ecx]
        xor     dl, byte ptr[ebx]
        mov     byte ptr[eax], dl
        inc     ecx
        inc     ebx
        inc     eax
        dec     esi
        jnz     make_file
        xor     eax, eax
        xor     ebx, ebx
        xor     ecx, ecx
        xor     edx, edx
        xor     esi, esi
        xor     edi, edi
        mov     edx, 10
        mov     esi, offset fil1array
        mov     edi, offset fil2array
        mov     ecx, 80h
lala:
        mov     al, byte ptr[esi]
        mov     bl, al
        and     al, 0fh
        and     bl, 0f0h
        cmp     al, 0Ah
        jl      zuzu
        add     al, 37h
        jmp     iuiu
zuzu:
        add     al, 30h
iuiu:
        ror     ebx, 4
        cmp     bl, 0Ah
        jl      zuzu2
        add     bl, 37h
        jmp     iuiu2
zuzu2:
        add     bl, 30h

```

```

iuiu2:
    mov     byte ptr[edi], bl
    inc     edi
    mov     byte ptr[edi], al
    inc     edi
    inc     esi
    dec     ecx
    jnz     lala
    invoke  CreateFileA, ADDR fname, GENERIC_WRITE + GENERIC_READ,
            NULL, NULL, CREATE_ALWAYS, FILE_ATTRIBUTE_NORMAL, NULL
    mov     fhandle, eax
    invoke  WriteFile, fhandle, ADDR fil2array, 256, ADDR bread, 0
    invoke  CloseHandle, fhandle
    mov     eax, offset ser_array
    mov     byte ptr[eax+16], 0
    invoke  SetDlgItemTextA, _hDlg, ID_EDITSERIAL, ADDR ser_array
exit_proc:
    mov     eax, 1
    ret
MakeKey   ENDP
end main

; keymaker.rc
#include "\masm32\include\resource.h"
#define ID_KeyGenDlg 103
#define ID_EDITNAME 1000
#define ID_EDITSERIAL 1001
#define ID_STATIC -1

MAINDLG DIALOGEX DISCARDABLE 0, 0, 160, 75
STYLE DS_3DLOOK | DS_CENTER | WS_POPUP | WS_VISIBLE | WS_CAPTION |
      WS_SYSMENU | WS_EX_CLIENTEDGE | WS_DLGMFRAME
CAPTION "*KeyMaker* for f0dders crkme #2*"
FONT 8, "MS Sans Serif"
BEGIN
    DEFPUSHBUTTON "&Randomize!", IDOK, 10, 10, 60, 12
    EDITTEXT ID_EDITSERIAL, 10, 40, 140, 12, ES_READONLY | ES_CENTER
    GROUPBOX "Serial:", ID_STATIC, 5, 30, 150, 25
    CTEXT "Coded by Cardenal Mendoza [01/29/2000]", ID_STATIC, 5,
        60, 150, 10, SS_SUNKEN | WS_DISABLED
END

; makefile
NAME = keymaker
OBSJ = $(NAME).obj
RES = $(NAME).res

```

```
$(NAME).EXE:$(OBJS) $(RES)
link /SUBSYSTEM:WINDOWS,4.0 $(OBJS) $(RES)

.asm.obj:
ml /c /coff $(NAME).asm

.rc.res:
rc $(NAME).rc
```

6 Appendix II - +spath's mail

Hi mendo,
 Ok, herets how I see the problem:
 from what I understood you have something like this:

```
    mov     esi, offset StartArray
Eloop:
    xor     al, byte ptr[esi]
    rol     eax, 1
    inc     esi
    cmp     esi, offset(StartArray+127)
    jle     ELoop
```

The corresponding decrypt loop would be

```
    mov     esi, offset(StartArray+127)
Dloop:
    xor     al, byte ptr[esi]
    ror     eax, 1
    dec     esi
    cmp     esi, offset StartArray
    jge     DLoop
```

Now let me define some notations:

C is the resulting dword, C(n) is bit n of this dword

P is the starting dword (BADCODE ?), P(n) is bit n of this dword

T(n)(k) is bit k of the temporary value in EAX after decryption round n

K(x)(y) is bit y of byte x of the array

+ is XOR

You know C and P, and want to generate plenty of K values; let's say you fill the array with all random values, the you start decrypting; for the first round you have 32 equations:

$$T(1)(0) = C(1) + K(127)(1)$$

$$T(1)(1) = C(2) + K(127)(2)$$

..

$$T(1)(6) = C(7) + K(127)(7)$$

$$T(1)(7) = C(8)$$

..

$$T(1)(30) = C(31)$$

$$T(1)(31) = C(0) + K(127)(0)$$

for any round n you have (A):

$$T(n)(0) = T(n-1)(1) + K(128-n)(1)$$

$$T(n)(1) = T(n-1)(2) + K(128-n)(2)$$

..

$$T(n)(6) = T(n-1)(7) + K(128-n)(7)$$

$$T(n)(7) = T(n-1)(8)$$

..

$$T(n)(30) = T(n-1)(31)$$

$$T(n)(31) = T(n-1)(0) + K(128-n)(0)$$

with $T_0 = C$ and $T(128) = P$, so that at last you have:

$$P(0) = T(128)(0) = T(127)(1) + K(0)(1)$$

$$P(1) = T(128)(1) = T(127)(2) + K(0)(2)$$

..

but using (A) we can extend $P(0)$ as

$$P(0) = T(127)(1) + K(0)(1)$$

$$= T(126)(2) + K(1)(2) + K(0)(1)$$

$$= T(125)(3) + K(2)(3) + K(1)(2) + K(0)(1)$$

= ...

note that some parts will be easier, when the bit is in the range 8-31, for instance:

$$P(7) = T(127)(8)$$

$$= T(126)(9)$$

= ...

$$= T(104)(31)$$

$$= T(103)(0) + K(24)(0)$$

So basically any bit of P can be written as a combination of $T(103)$ and key bytes from $K(0)$ to $K(24)$; you can expand these equations a bit more until you get 32 equations describing each bit of P from $T(96)$ and $K(0) \dots K(31)$. If you decrypt with random K bytes until $T(96)$, you have 32 equations with 32 unknown variables.

> From here you can solve it using a gaussian pivot or a matrix inversion; a good idea would be to first use gaussian elimination to obtain a triangular matrix, so that you can easily calculate the determinant, which should give you constraints on some K bits. You can get infos about these methods at <http://www.geog.ubc.ca/numeric/labs/lab3/lab3/lab3.html>, this case is just slightly different since you work in $\mathbb{Z}/2\mathbb{Z}$.

regards, Spath.