# Casl-Ltl A Casl Extension for dynamic systems Summary

<b>CoFI Document:</b>	CASL/Summary			
Version: 1.0	8 August 2003			

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# Abstract

CASL the basic language developed within CoFI, the Common Framework Initiative for algebraic specification and development, cannot be used for specifying the requirements and the design of dynamic software systems. CASL-LTL is an extension to overcome this limit, allowing to specify dynamic system by modelling them by means of labelled transition systems and by expressing their properties with temporal formulae. It is based on LTL, the Labelled Transition Logic, that is a logicalgebraic formalism for the specification of dynamic systems, mainly developed by E.Astesiano and G. Reggio (see [AR01] and [CR97]).

This document gives a detailed summary of the syntax and intended semantics of CASL-LTL. It is intended for readers who are already familiar with CASL ([Mos03]).

Four short examples are given in the appendix, and extended case studies using CASL-LTL are given in [CR00, CR03]. An extensive companion user method is given in [CR03] (while [CR00] gives a first attempt to rely on structuring concepts). CASL-LTL was also used to present the semantics of some parts of UML in [RACH00, RCA01].

<sup>\*...</sup> †

# Chapter 1

# Casl-Ltl

[ABR99] present different ways of exploiting algebraic methods in concurrency. The CASL-LTL extension (A3 "algebraic specifications of dynamicdata types" approach of [ABR99]) uses dynamic sorts, the elements of which correspond to concurrent systems. It is based on LTL, the Labelled Transition Logic, that is a logic-algebraic formalism for the specification of dynamic systems, mainly developed by E.Astesiano and G. Reggio (see [AR01] and [CR97]). While [CR97] explains the differences with the temporal logics developed in [MP89, MP92] (e.g., LTL is branching-time instead of linear), the connectors and formula of LTL are close to those of CTL\* [Eme90], and LTL is anchored (cf. footnote 1 page 4), first-order many-sorted and provides also edge formulas.

# **1.1 Basic Concepts**

CASL-LTL is an extension of CASL for the specification of what we call in a general way *dynamic systems*, as processes, concurrent, reactive, distributed, parallel, ... systems. The basic idea behind CASL-LTL is to model a dynamic system by using a labelled transition system.

A labelled transition system (shortly *lts*) is a triple (*STATE*, *LABEL*,  $\rightarrow$ ), where *STATE* and *LABEL* are two sets, and  $\rightarrow \subseteq STATE \times LABEL \times STATE$  is the transition relation. A triple  $(s, l, s') \in \rightarrow$  is said to be a transition and is usually written  $s \stackrel{l}{\longrightarrow} s'$ .

Given an lts we can associate with each  $s_0 \in STATE$  the tree (transition tree) whose root is  $s_0$ , where if it has a node *n* decorated with *s* and  $s \stackrel{l}{\longrightarrow} s'$ , then it has a node *n'* decorated with *s'* and an arc decorated with *l* from

n to n', the order of the branches is not considered, and two identically decorated subtrees with the same root are considered as a unique subtree.

We model a dynamic system S with a transition tree determined by an lts

$$(STATE, LABEL, \rightarrow)$$

and an initial state  $s_0 \in STATE$ ; the nodes in the tree represent the intermediate (interesting) situations of the life of S, and the arcs of the tree the possibilities of S of passing from one situation to another. It is important to note here that an arc (a transition)  $s \stackrel{l}{\longrightarrow} s'$  has the following meaning: S in the situation s has the *capability* of passing into the situation s' by performing a transition, where the label l represents the interaction with the environment during such a move; thus l contains information on the conditions on the environment for the capability to become effective, and on the transformation of such environment induced by the execution of the transition.

An lts may be specified by an algebraic specification having two sorts,

whose elements are the states and the labels of the lts respectively, and a ternary predicate

$$\_--\_->\_: State \times Label \times State$$

corresponding to the transition relation.

The basic idea behind CASL-LTL is to add to CASL a special construct to declare such two sorts and the associate predicate that correspond to an lts; precisely the declaration of *dynamic sort* 

#### dsort Ds label\_Ds

where Ds is called a *dynamic sort* and  $Label_Ds$  is its label sort. This terminology wants to remind that the elements of Ds are dynamic, indeed they correspond to a dynamic system in a particular initial situation.

dsort Ds label Label\_Ds corresponds to the following declarations

sorts Ds,  $Label_Ds$ pred \_\_\_\_\_:  $Ds \times Label_Ds \times Ds$ .

The CASL formulae (many sorted first order logic) built by using the transition predicate  $(\_--\_->\_)$  allows to express some properties on the behaviour of a dynamic system, but they are not sufficient. For example, using such formulae we cannot state liveness properties as, "eventually the system will send out some value" (i.e., eventually it will perform a transition whose label correspond to send out such value). Instead such properties could be easily expressed by using some kind of temporal logic. Thus CASL-LTL includes temporal logic combinators, and precisely those of the many-sorted first-order temporal logic of [CR97]. Clearly, the temporal formulae are sensible only when referring to elements of dynamic sorts.

# 1.2 Dynamic Signatures

A dynamic many-sorted signature  $D\Sigma = (S, DS, TF, PF, P)$  consists of:

- a set S of sorts;
- a set DS of dynamic sorts s.t.  $DS \subseteq S$  and for all  $Ds \in DS$  there exists  $Label_Ds \in S DS$ ;
- sets  $TF_{w,s}$ ,  $PF_{w,s}$ , of total function symbols, respectively partial function symbols, such that  $TF_{w,s} \cap PF_{w,s} = \emptyset$ , for each function profile (w, s) consisting of a sequence of argument sorts  $w \in S^*$  and a result sort  $s \in S$ ;
- sets P<sub>w</sub> of predicate symbols, for each predicate profile consisting of a sequence of argument sorts w ∈ S<sup>\*</sup>, s.t. for each Ds ∈ DS \_\_\_\_ ∈ P<sub>Ds Label\_Ds Ds</sub>.

A dynamic many-sorted signature morphism

$$\sigma: (S, DS, TF, PF, P) \to (S', DS'TF', PF', P')$$

consists of a mapping from S to S', and for each  $w \in S^*, s \in S$ , a mapping between the corresponding sets of function, resp. predicate symbols, s.t. dynamic sorts are sent into dynamic sorts, and the associated label sort and transition predicate are sent into the corresponding label sort and transition predicate. Precisely:

$$\sigma(Label_Ds) = Label_\sigma(Ds) \text{ and}$$
  
$$\sigma(\_--->\_: Ds \times Label_Ds \times Ds) = \_--->\_: \sigma(Ds) \times Label_\sigma(Ds) \times \sigma(Ds).$$

## 1.3 Models

Assume that  $D\Sigma = (S, DS, TF, PF, P)$  is a dynamic many-sorted signature.

A dynamic many-sorted model for  $D\Sigma$   $M \in \mathbf{Mod}(D\Sigma)$  is defined as for the basic CASL.

A (weak) dynamic many-sorted homomorphism h from  $M_1$  to  $M_2$ , with  $M_1, M_2 \in \mathbf{Mod}(D\Sigma)$  is defined as for the basic CASL.

However, the explicit presence of the dynamic sorts allows us to equip a dynamic model M with a set of "paths" for each dynamic sort Ds representing the possible behaviours of the elements of sort Ds in M.

Paths are defined precisely as follows. For each  $M \in \mathbf{Mod}(D\Sigma)$  and  $Ds \in$ DS, the set of the paths on M of sort Ds, denoted by PATH(M, Ds), is the set of all the sequences of transitions having the form either (1) or (2) below:

- (1)
- (2)

where for all  $i \ge 0$ ,  $s_i \in Ds^M$ ,  $l_i \in Label_Ds^M$ ,  $(s_i, l_i, s_{i+1}) \in \mathcal{M}$ , and there do not exist  $l, \bar{s'}$  such that  $(s_n, l, s') \in \mathcal{M}$ .

If  $\sigma = s_0 \ l_0 \ s_1 \ l_1 \ s_2 \ l_2 \ \dots$  and  $\sigma \in PATH(M, Ds)$ - given  $h \ge 0$ , if there exists  $s_h$ , then  $\sigma|_h$  denotes the path  $s_h l_h s_{h+1} l_{h+1} s_{h+2} \ldots$ and is referred to as " $\sigma$  at point h", otherwise it is undefined, - first\_state( $\sigma$ ) denotes  $s_{\theta}$ , the first state of  $\sigma$ , and first\_label( $\sigma$ ) denotes  $l_{\theta}$ , the first label of  $\sigma$ , if exists, i.e., if  $\sigma$  is not just a state.

#### 1.4Sentences

For a dynamic many-sorted signature  $D\Sigma = (S, DS, TF, PF, P)$  the dynamic many-sorted sentences in  $\mathbf{TSen}(D\Sigma)$  are the usual closed manysorted first-order logic formulae, built from atomic formulae using quantification (over sorted variables) and logical connectives plus temporal formulae anchored to the elements of the dynamic sorts.

The temporal formulae of CASL-LTL express properties of the elements of a dynamic sort Ds (dynamic elements) in terms of their paths, i.e., of their possible behaviours. Such temporal formulae have form

 $in_one_case(t,\pi)$ either  $in_any_case(t,\pi)$ or

where t is a term of sort Ds, and  $\pi$  a path formula. The first formula can be read as "for every path  $\sigma$  starting in the state denoted by t,  $\pi$  holds on  $\sigma$ ". while the second means "there exists a path  $\sigma$  starting in the state denoted by t s.t.  $\pi$  holds on  $\sigma$ ".<sup>1</sup> The path formulae for the elements of a dynamic

<sup>&</sup>lt;sup>1</sup>We anchor these formulae to states, following the ideas in [MP89]. The major difference with the classical temporal logic is that we do not specify a single system but, in general, one or many types of systems, so there is not a single initial state but several, hence the need for an explicit reference to states (through terms) in the formulae built with in\_any\_case.

sort Ds express properties on its paths, i.e., on the possible behaviours of the elements of Ds.

The dynamic sentences in  $\mathbf{TSen}(D\Sigma)$  and the path formulae for the elements of the various dynamic sorts of  $D\Sigma$  ( $\mathbf{PSen}(D\Sigma, Ds)_{Ds \in DS}$ ) are defined as follows:

**TSen** $(D\Sigma)$  contains all the atomic formulae of the basic CASL, all those built with the logic combinator of the basic CASL, and the following temporal formulae: for each  $Ds \in DS$ 

 $in\_any\_case(t,\pi)$  and  $in\_one\_case(t,\pi)$ 

with t term of sort Ds and  $\pi \in \mathbf{PSen}(D\Sigma, Ds)$ .

The path formulae over  $D\Sigma$  for the elements of sort Ds,  $\mathbf{PSen}(D\Sigma, Ds)$ , are defined as follows

$$- [x \bullet F] \qquad x \text{ variable of sort } Ds, F \in \mathbf{TSen}(D\Sigma)$$

This formula holds on a path  $\sigma$  whenever F holds at the first state of  $\sigma$ .

$$- \langle x \bullet F \rangle$$
 x variable of sort Label\_Ds,  $F \in \mathbf{TSen}(D\Sigma)$ 

This formula holds on a path  $\sigma$  whenever  $\sigma$  is not just a single state and F holds at the first label of  $\sigma$ .

$$-\pi_1 until \pi_2 \qquad \pi_1, \pi_2 \in \mathbf{PSen}(D\Sigma, Ds)$$

This formula holds on a path  $\sigma$  whenever there exists a point in  $\sigma$  s.t.  $\pi_2$  holds at such point and  $\pi_1$  holds until before it.

$$- next \ \pi \qquad \qquad \pi \in \mathbf{PSen}(D\Sigma, Ds)$$

This formula holds on a path  $\sigma$  whenever  $\pi$  holds at  $\sigma$  at point 1 if it exists or whenever  $\sigma$  at point 1 does not exist.

- eventually  $\pi$ 

 $\pi \in \mathbf{PSen}(D\Sigma, Ds)$ 

This formula holds on a path  $\sigma$  whenever there exists a point in  $\sigma$  s.t.  $\pi$  holds at such point.

 $- always \ \pi \qquad \qquad \pi \in \mathbf{PSen}(D\Sigma, Ds)$ 

This formula holds on a path  $\sigma$  whenever  $\pi$  holds at any point in  $\sigma$ .

 $- \neg \pi, \pi \Rightarrow \pi', \forall y \bullet \pi$ 

y variable of whatever sort,  $\pi, \pi' \in \mathbf{PSen}(D\Sigma, Ds)$ 

with the usual meaning

## **1.5** Satisfaction

Let M be a dynamic model over  $D\Sigma$  and v a variable evaluation, then we define by multiple induction:

- the validity of a dynamic formula  $F \in \mathbf{TSen}(D\Sigma)$  in M w.r.t. v (written  $M, v \models F$ ),
- the validity of a path formula  $\pi \in \mathbf{PSen}(D\Sigma, Ds)$  on a path  $\sigma \in PATH(D\Sigma, Ds)$  in M w.r.t. v (written  $M, v, \sigma \models \pi$ ),

as follows:

- $M, v \models in\_any\_case(t,\pi)$  iff for each  $\sigma \in PATH(M, Ds)$  such that  $first\_state(\sigma) = t^{M,v}, M, v, \sigma \models \pi$
- $M, v \models in\_one\_case(t, \pi)$  iff there exists  $\sigma \in PATH(M, Ds)$  such that  $first\_state(\sigma) = t^{M,v}$  and  $M, v, \sigma \models \pi$
- $-M, v, \sigma \models [x \bullet F]$  iff  $M, v[first\_state(\sigma)/x] \models F$
- $-M, v, \sigma \models < x \bullet F >$ iff

 $first\_label(\sigma)$  is defined and  $M, v[first\_label(\sigma)/x] \models F$ 

- $\begin{array}{l} -M, v, \sigma \models \pi_1 \ until \ \pi_2 \ \text{ iff there exists } j \ge 0 \ \text{such that} \ \text{ for all } h, \\ 0 < h < j, \ M, v, \sigma|_h \models \pi_1 \ \text{and} \ M, v, \sigma|_j \models \pi_2 \end{array}$
- $M, v, \sigma \models next \pi$  iff  $\sigma|_1$  undefined or  $\sigma|_1$  defined and  $M, v, \sigma|_1 \models \pi$
- $M, v, \sigma \models eventually \pi$  iff there exists  $j \ge 0$  such that  $M, v, \sigma \mid_j \models \pi$
- $\begin{array}{c|c} & M, v, \sigma \models always \ \pi \ \text{iff for all} \ j \geq 0 \ \text{such that} \ \sigma|_j \ \text{is defined}, \ M, v, \sigma|_j \models \\ \pi \end{array}$
- $\ \neg \ F, \ F \ \Rightarrow \ F', \ \forall \ x \bullet F, \ \neg \ \pi, \ \pi \ \Rightarrow \ \pi', \ \forall \ x \bullet \pi \ \text{as usual}.$

# **1.6 Basic Constructs**

This section indicates the abstract and concrete syntax of the new constructs introduced by CASL-LTL to the basic specifications, and describes their intended interpretation.

#### 1.6.1 Dynamic Sort

SORT-ITEM ::= dsort-item SORT-ITEM SORT-ITEM

A dynamic sort declaration is written:

#### dsort Ds label Label\_Ds

and implicitely corresponds to the following declarations

sorts Ds,  $Label_Ds$ pred \_\_\_\_\_:  $Ds \times Label_Ds \times Ds$ .

## 1.7 Axioms

FORMULA ::= TEMPORAL

A CASL-LTL formula may be also a temporal formula.

#### 1.7.1 Temporal Formulae

TEMPORAL	::=	temporal	PATH-QUANTIFIER	TERM	PATH-FORMULA
PATH-QUANTIFIER	::=	anycase	onecase		

A temporal formula with the anycase quantifier is written:

 $in\_any\_case(T, PF)$ 

A temporal formula with the onecase quantifier is written:

 $in\_one\_case(T, PF)$ 

The first case is the universal path quantification, holding when PF holds for all paths starting from the element represented by the term T; the second case is the existential path quantification, holding when PF holds for at least one path starting from the element represented by T.

#### 1.7.2 Path Formulae

These formulae represent properties on the paths, i.e., on the possible behaviours of the dynamic elements.

PATH-FORMULA ::= STATE-COND | LABEL-COND | UNTIL | NEXT | EVENTUALLY | ALWAYS | P-QUANTIFICATION | P-CONJUNCTION | P-DISJUNCTION | P-IMPLICATION | P-EQUIVALENCE | P-NEGATION

#### 1.7.2.1 State Condition

STATE-COND ::= state-cond VAR-DECL FORMULA

A state condition is written:

 $[VD \bullet F]$ 

#### 1.7.2.2 Label Condition

LABEL-COND ::= label-cond VAR-DECL FORMULA

A label condition is written:

 $< VD \bullet F >$ 

#### 1.7.2.3 Until

UNTIL ::= until PATH-FORMULA PATH-FORMULA

#### An until formula is written:

PF<sub>1</sub> until PF<sub>2</sub>

#### 1.7.2.4 Next

NEXT ::= next PATH-FORMULA

A next formula is written:

 $next \ PF$ 

#### 1.7.2.5 Eventually

EVENTUALLY ::= eventually PATH-FORMULA

An eventually formula is written: eventually PF

#### 1.7.2.6 Always

ALWAYS ::= always PATH-FORMULA

An always formula is written:

always PF

#### 1.7.2.7 First order combinators on path formulae

```
P-QUANTIFICATION::= pquantification QUANTIFIER VAR-DECL+ PATH-FORMULAP-CONJUNCTION::= pconjunction PATH-FORMULA+P-DISJUNCTION::= pdisjunction PATH-FORMULA+P-IMPLICATION::= pimplication PATH-FORMULA PATH-FORMULAP-EQUIVALENCE::= pequivalence PATH-FORMULA PATH-FORMULAP-NEGATION::= pnegation PATH-FORMULA
```

These formulae are written as the corresponding one of the basic CASL.

# **1.8 Structured Specifications**

The structuring constructs of CASL-LTL are exactly the same of the basic CASL, clearly defined using the new signature morphisms, which preserve dynamicity of sorts, and the associated labels sorts and transition predicates (see [CR97] for the precise definitions).

# **1.9** Architectural Specifications

The relationship of the new constructs of CASL-LTL with the architectural specifications need further investigations.

# 1.10 Specification Libraries

As for the basic CASL.

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# .1 Abstract Syntax

The abstract syntax of CASL-LTL is given by extending with the following clauses the part concerning basic specifications of that the basic CASL (see [Mos03]).

SORT-ITEM	::=	dsort-item SORT-ITEM SORT-ITEM
FORMULA	::=	TEMPORAL
TEMPORAL PATH-QUANTIFIER	::= ::=	temporal PATH-QUANTIFIER TERM PATH-FORMULA anycase   onecase
PATH-FORMULA	::=	STATE-COND   LABEL-COND   UNTIL   NEXT   EVENTUALLY   ALWAYS   P-QUANTIFICATION   P-CONJUNCTION   P-DISJUNCTION   P-IMPLICATION   P-EQUIVALENCE   P-NEGATION
STATE-COND	::=	state-cond VAR-DECL FORMULA
LABEL-COND	: :=	label-cond VAR-DECL FORMULA
UNTIL	: :=	until PATH-FORMULA PATH-FORMULA
NEXT	: :=	next PATH-FORMULA
EVENTUALLY	: :=	eventually PATH-FORMULA
ALWAYS	: :=	always PATH-FORMULA
P-QUANTIFICATION	: :=	pquantification QUANTIFIER VAR-DECL+ PATH-FORMULA
P-CONJUNCTION	: :=	pconjunction PATH-FORMULA+
P-DIS JUNCTION	: :=	pdisjunction PATH-FORMULA+
P-IMPLICATION	::=	pimplication PATH-FORMULA PATH-FORMULA
P-EQUIVALENCE	::=	pequivalence PATH-FORMULA PATH-FORMULA
P-NEGATION	: :=	pnegation PATH-FORMULA

# .2 Abbreviated Abstract Syntax

The abbreviated abstract syntax of CASL-LTL is given by extending with the following clauses the part concerning basic and subsorted specifications of that the basic CASL (see [Mos03]).

SIG-ITEM	::= dso	rt-item SORT-ITEM SOF	RT-ITEM
FORMULA	::= tem	poral PATH-QUANTIFIEF	A TERM PATH-FORMULA
PATH-QUANTIFIER	::= any	case   onecase	
PATH-FORMULA	::= sta lab unt nex eve	te-cond VAR-DECL FORM el-cond VAR-DECL FORM il PATH-FORMULA PATH- t PATH-FORMULA   ntually PATH-FORMULA	IULA   IULA   -FORMULA   

```
always PATH-FORMULA |

pquantification QUANTIFIER VAR-DECL+ PATH-FORMULA |

pconjunction PATH-FORMULA+ |

pdisjunction PATH-FORMULA+ |

pimplication PATH-FORMULA PATH-FORMULA |

pequivalence PATH-FORMULA PATH-FORMULA |

pnegation PATH-FORMULA
```

# .3 Concrete Syntax

The concrete syntax of CASL-LTL is given by extending with the following clauses the part concerning basic specifications with subsorts of that the basic CASL (see [Mos03]).

SIG-ITEM ::= dsort SORT-ITEM label SORT-ITEM ; FORMULA ::= PATH-QUANTIFIER "(" TERM "." PATH-FORMULA ")" PATH-QUANTIFIER ::= in\_any\_case | in\_one\_case PATH-FORMULA ::= "[" VAR-DECL "." PATH-FORMULA "]" | "<" VAR-DECL "." PATH-FORMULA ">" | PATH-FORMULA until PATH-FORMULA | next PATH-FORMULA eventually PATH-FORMULA always PATH-FORMULA QUANTIFIER VAR-DECL ;...; VAR-DECL "." PATH-FORMULA PATH-FORMULA /\ PATH-FORMULA /\.../\ PATH-FORMULA | PATH-FORMULA \/ PATH-FORMULA \/...\/ PATH-FORMULA | PATH-FORMULA => PATH-FORMULA | PATH-FORMULA if PATH-FORMULA PATH-FORMULA <=> PATH-FORMULA | not PATH-FORMULA true false

# .4 Disambiguation

The context-free grammar given in Section .3 for input syntax is quite ambiguous. This section explains various precedence rules for disambiguation, and the intended grouping of mixfix formulae and terms (which are to be recognized in a separate phrase, dependent on the declared symbols and parsing annotations).

Within a FORMULA, the use of the new path quantifiers (in\_any\_case and in\_one\_case) do not cause any problem, due to the fact that they have a "functional syntax".

Within a PATH-FORMULA, the use of prefix and infix notation for the logical connectives gives rise to some potential ambiguities. These are resolved as follows:

- the state and label condition combinators ([ . ] and < . >) do not cause any problem, due to the fact that have a "functional syntax".
- The first-order logical connectives have a precedence higher than any temporal combinator, and their relative precedences are as in basic CASL (see [Mos03]).

'PATH-FORMULA until PATH-FORMULA' has the highest precedence; and when repeated, 'until' groups to the right;

- 'always PATH-FORMULA' has lower precedence;
- 'eventually PATH-FORMULA' has even lower precedence.

For what concerns the implicit mix-fix predicates associated with dynamic sorts  $(\_ -- \_ -> \_)$  have the lowest precedence.

# .5 Lexical Syntax

The lexical syntax of CASL-LTL is as for the basic CASL, except that NO-BRACKET-SIGNS cannot be also one of the following *reserved symbols*:

-- --> < > [ ]

# .6 Display Format

The input symbols introduced in CASL-LTL in the following table are to be displayed as the mathematical symbols shown below them.

in_any_case	in_one_case	eventually	always	until	next	> _
$\bigtriangleup$	$\bigtriangledown$	$\diamond$		$\mathcal{U}$	0	$\_$

## .7 Example 1: CCS

**spec** CHANNEL = **free type** Channel ::=  $\alpha \mid \beta \mid \gamma \mid \eta \mid \ldots$ spec CCS =CHANNEL then free { types Behaviour ::= nil | \_\_\_\_(Label\_Behaviour; Behaviour) |  $\_+\_(Behaviour; Behaviour) | \_||\_(Behaviour; Behaviour);$ Label\_Behaviour ::=  $\_!(Channel) \mid \_?(Channel) \mid \tau$ dsort Behaviour label Label\_Behaviour  $ops \_ + \_$ : Behaviour  $\times$  Behaviour  $\rightarrow$  Behaviour assoc; comm; idem; unit: nil  $||_: Behaviour \times Behaviour \rightarrow Behaviour$  assoc; comm; **vars**  $B, B_1, B_2, B'_1, B'_2$ : Behaviour; C: Channel; L: Label\_Behaviour;  $L.B \xrightarrow{L} B$ • •  $B_1 \xrightarrow{L} B'_1 \Rightarrow B_1 + B_2 \xrightarrow{L} B'_1$  $B_1 \xrightarrow{L} B'_1 \Rightarrow B_1 || B_2 \xrightarrow{L} B'_1 || B_2$  $B_1 \xrightarrow{C!} B'_1 \wedge B_2 \xrightarrow{C?} B'_2 \Rightarrow B_1 || B_2 \xrightarrow{\tau} B'_1 || B'_2$ } end

Note that, given the properties (associativity, commutativity, ...) declared for the  $\_-+\_$  and  $\_||\_$  operations, fewer axioms are needed to describe the transition relation than in the original CCS description [Mil80].

#### .8 Example 2: Fancy processes

spec PROC =
INT then
dsort Proc label Label\_Proc
preds rec?, send? : Int × Label\_Proc
%% checks whether a label corresponds to receive/send an integer
vars P, P': Proc; I : Int; L, Y : Label\_Proc
•  $P \xrightarrow{L} P' \land (\neg I = 0) \land rec?(L, I) \Rightarrow$ in\_any\_case(P', eventually (< Y • send?(I + 1, Y) > \land
 eventually < Y • send?(I + 2, Y) >))
%% if a process receives a non-zero integer I, then in any case eventually
%% (it will send out I+1 and eventually also I+2)

•  $P \xrightarrow{L} P' \land rec?(L, \theta) \Rightarrow$  $in\_any\_case(P', always < Y \bullet (\neg send?(\theta, Y)) \land (\neg rec?(\theta, Y)) >)$ 

%% if a process receive 0, then in any case forever it will never send out or receive 0

## .9 Example 3: A Fancy Concurrent System

```
spec CSYSTEM =
    PROC then
free {
    types System ::= \emptyset \mid \_\_||\_\_(Proc; System)
        Label_System ::= I(Int) \mid O(Int) \mid \tau
    dsort System label Label_System
}
vars P, P': Proc; I : Int; Y : Label_Proc; S : System; Z : Label_System
• P \mid |P' \mid |S = P' \mid |P \mid |S
• in_one_case(P, eventually < Y • send?(I, Y) >) \Rightarrow
    in_one_case(P ||S, eventually < Z • Z = O(I) >)
%% if a process component of the system has at least in a case the capability
%% to eventually send out I, then also the system has such capability
```

# .10 Example 4: A Buffer (The Bit example)

This example is a very simple concurrent system consisting of a buffer and a user. It is taken from [ABR99] and its specification is now expressed in CASL-LTL.

The system **Bit** (called Bit since it is really very small) consists of two components in parallel: a user and a buffer. The buffer is organized as a queue and contains integers; it may obviously receive and return integer values; it may break down, in which case its content will be  $10^{10}$ , and, moreover, it may happen that the last element of its content is duplicated.

When the system is started by the environment, the buffer is empty and the user puts in sequence 0 and 1 on the buffer; then it gets the first element from the buffer. If this element is the number  $\theta$  the user must inform the environment of the correct working of the buffer, otherwise it must signal that there is an error.

Thus **Bit** is an interactive concurrent system with components having both autonomous activities (as the buffer failures) and cooperations (the user writing/reading the buffer), and using some static data (integers); furthermore it also has some relevant static/functional aspects, as the queue organization of the buffer.

Some relevant requirements on **Bit** are:

- R0 The buffer must always be able to receive any integer value.
- **R1** When the user is terminated, it cannot perform an activity again.
- **R2** In at least one case, the system must behave correctly.

- **R3** After being started, it will eventually signal ok or error
- **R4** *ok* and *error* are signaled at most once, and it cannot happen that both are signaled.
- **R5** The user puts integers on and gets integers from the buffer.

We first specify the two components of the system, the buffer and the user, and then how they cooperate.

```
spec BUFFER =
      INT_QUEUE with sort Queue \mapsto Buffer then
      dsort Buffer label Lab_Buffer
      ops \tau :\rightarrow Lab\_Buffer
            receive, return : Int \rightarrow Lab\_Buffer
      vars B: Buffer; I: Int
            \mathit{not\_empty}(B) \Rightarrow B \xrightarrow{\mathit{return}(\mathit{first}(B))} \mathit{remove}(B)
            B \xrightarrow{receive(I)} put(I, B)
            B \xrightarrow{\tau} put(10^{10}, empty)
            not\_empty(B) \Rightarrow B \xrightarrow{\tau} dup(B)
spec USER_STATUS =
      INT then
      sort User_Status
      ops initial, putting_0, putting_1, reading, terminated : \rightarrow User_Status
            read: Int \rightarrow User\_Status
spec USER =
      USER_STATUS with sort User\_Status \mapsto User then
      dsort User label lab_User
      ops start, ok, error :\rightarrow lab\_User
            put, get : Int \rightarrow lab\_User
      vars I:Int
            initial \xrightarrow{start} putting_0
            putting_0 \xrightarrow{put(0)} putting_1
            putting_1 \xrightarrow{put(1)} reading
            reading \xrightarrow{get(I)} read(I)
            read(0) \xrightarrow{ok} terminated
            \textit{not\_eq}(I, \theta) \Rightarrow \textit{read}(I) \xrightarrow{\textit{error}} \textit{terminated}
spec System =
      BUFFER and USER then
      dsort System label Lab_System
      ops \_ | \_: Buffer \times User \rightarrow System
            start, ok, error, \tau :\rightarrow Lab\_System
      vars B, B': Buffer; U, U': User
            U \xrightarrow{start} U' \Rightarrow empty \ | \ U \xrightarrow{start} empty \ | \ U'
            B \xrightarrow{receive(I)} B' \land \ U \xrightarrow{put(I)} U' \Rightarrow B \mid U \xrightarrow{\tau} B' \mid U'
```