

# Functions

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	<i>TITLE :</i> Functions	
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# Chapter 1

# Functions

## 1.1 Functions

Functions :

[Click here](#) for the main documentation.

Laplace offers a lot (really? ;-) internal functions. Call them with the parameters separated by commas embedded in () brackets, e.g.

`sin(pi)`

`exp(1)`

`parameter : ...` means that the parameter must evaluate to one of the given object types.

`result : ...` means that the result is of the given object types. If there are more than one type, each type corresponds to a type in the parameter.

`abs(expr)`

`acos(expr)`

`acosh(expr)`

`acot(expr)`

`addrows(matrix,row1,row2,expr)`

`asin(expr)`

`asinh(expr)`

`atan(expr)`

`atanh(expr)`

`combine(list)`

`const(list)`

`cos(expr)`

`cosh(expr)`

`cot(expr)`

`debug(string)`

`det(expr)`

`diff(function,variable)`

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dispose(list)  
disposeall()  
do(list)  
eq(expr,expr)  
eqleft(eq)  
eqright(eq)  
eval(expr)  
exp(expr)  
fak(expr)  
include(path)  
inv(expr)  
ln(expr)  
log(expr)  
matrix([list],[list],...)  
multrow(matrix,row1,expr)  
neg(expr)  
rang(expr)  
sign(expr)  
sin(expr)  
sinh(expr)  
solve(expr)  
spur(expr)  
sqrt(expr)  
swaprows(matrix,row1,row2)  
tan(expr)  
tanh(expr)  
taylor(function,a,grade)  
trans(expr)  
umatrix(size)  
vector(list)  
window(reference)

## 1.2 Trigonometric functions

sin(expression) :  
cos(expression) :  
tan(expression) :  
cot(expression) :  
asin(expression) :

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acos(expression) :  
atan(expression) :  
acot(expression) :  
sinh(expression) :  
cosh(expression) :  
tanh(expression) :  
asinh(expression) :  
acosh(expression) :  
atanh(expression) :  
expression : real, equation  
result : real, equation

Calculate those well known trigonometric functions.

### 1.3 Functions - abs

abs(expression) :  
expression : real, vector, equation  
result : real, vector, equation

Real : Returns the absolute of the real.

Vector : Returns the absolute of the vector, which is defined as  $\sqrt{a_1^2 + a_2^2 + \dots}$  where  $a_1, a_2$  are the components of the vector. (Physically this is the length of the vector.)

### 1.4 Functions - addrows

addrows(matrix,r1,r2,expression) :  
matrix : matrix (must be variable or parameter)  
r1 : real (should be integer)  
r2 : real (should be integer)  
expression : real  
result : matrix

This will copy the input matrix, except that row r1 will be replace by (row r1)+expression\*(row r2)

### 1.5 Functions - combine

combine(list) :  
result : matrix  
List is a list of object names of vectors or matrices (may be mixed).  
This will create a matrix that is a combination of the input vectors/matrices. E.g.

```
combine(matrix([1,2],[3,4]),vector(a,b))
```

```
/1 3 a\  
\2 4 b/
```

---

## 1.6 Functions - const

const(list) :

List is a list of object names separated by commas, where name is name[:type] the object name with an optional type specifier :

r, real - real object (default)

v, vec, vector - vector object, any dimension

v[d], vec[d], vector[d] - vector object, dimension d

m, mat, matrix - matrix object, any size

m[r,c], mat[r,c], matrix[r,c] - matrix object, size r\*s

const() will create the named objects.

## 1.7 Functions - debug

debug(string) :

This will add the string to the debug list.

## 1.8 Functions - det

det(expression) :

expression : matrix, equation

result : real, equation

Returns the determinant of the matrix.

## 1.9 Functions - diff

diff(function,variable) :

This will calculate the first derivation of the given function.

There are different kinds of syntax for this command :

1) Calculate the derivation of an already defined function of one variable :

diff(functionname) - e.g.

f(x)=x<sup>2</sup>

diff( f )

2) Calculate the (partial) derivation of an already defined function of one or more variables :

diff(functionname,variable) - e.g.

f(x,y)=x<sup>2</sup>+y<sup>3</sup>

diff( f , x )

diff( f , y )

3) Calculate the (partial) derivation of an already defined function of two or more variables, setting some variable to constant values :

diff(functionname(parameterlist),variable) - e.g.

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$f(x,y)=x^2+y^3*x$

`diff( f(x,1) , x )`

`g(x)=diff( f(x,y) , y )`

4) Calculate the (partial) derivation of an explicit given function of one or more variables :

`diff((expression),variable) - e.g.`

`diff( (x^2*sin(x)) , x )`

Don't forget the brackets, otherwise Laplace cannot realize, that this is not a reference.

Usually a function has free variables x, y or z. If you want to other variable names, you have to declare them as **constants** before using `diff()`, or use `diff()` inside of a function definition. E.g.

`diff((urps^2*sin(urps)),urps) -> Error : undefined reference.`

use instead :

`const(urps)`

`diff( (urps^2*sin(urps)) , urps )`

or

`f(urps)=diff( (urps^2*sin(urps)) , urps )`

## 1.10 Functions - dispose

`dispose(list) :`

This will dispose the previously defined objects. List is a list of object names separated by commas.

## 1.11 Functions - disposeall

`disposeall() :`

This will dispose all previously defined objects.

## 1.12 Functions - do

`do(list) :`

This is a synonym for an expression list. E.g.

`{debug("Hello world !"), sin(2)}` and

`do(debug("Hello world !"), sin(2))` are equal.

## 1.13 Functions - eq

`eq(expression, expression) :`

expression : real, vector, matrix

result : equation

This will create an equation object.

## 1.14 Functions - eqleft

eqleft(equation) :

Get the left side of an equation.

## 1.15 Functions - eqright

eqright(equation) :

Get the right side of an equation.

## 1.16 Functions - eval

eval(expression) :

expression : real, vector, matrix, equation

result : depends on expression

This will evaluate the given expression. Parameter references are replaced, too.

## 1.17 Functions - exp

exp(expression) :

expression : real, equation

result : real, equation

Returns  $e^x$  of the real. Use this functions instead of entering  $e^x$  directly

## 1.18 Functions - fak

fak(expression) :

expression : real, equation

result : real, equation

Returns  $x!$  (factorial) of a whole reals.  $x!$  for  $x \leq 0$  is 0.

## 1.19 Functions - include

include(path) :

This will load and process a file from the directory Include.

See also Libraries.

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## 1.20 Functions - inv

inv(expression) :

expression : real, matrix, equation

result : real, matrix, equation

Real : Return the invers of the real, which is simple  $1/x$

Matrix : Return the invers of the matrix, which is defined that  $m \cdot \text{inv}(m)$  is the standart matrix.

## 1.21 Functions - ln/log

ln(expression) :

log(expression) :

expression : real, equation

result : real, equation

Returns the natural/common logarithm of the real.

## 1.22 Functions - matrix

matrix([list],[list],...) :

This will create a matrix object. [list] is a column of the matrix, and list is a list of expressions seperated by commas. The components must evaluate to real. E.g.

```
matrix([1,2,3],[4,5,6],[7,8,9])
```

```
/1 4 7\
```

```
|2 5 8|
```

```
\3 6 9/
```

## 1.23 Functions - multrow

multrow(matrix,r,expression) :

matrix : matrix (must be variable or parameter)

r : real (should be integer)

expression : real

result : matrix

This will copy the input matrix, except that row r will be replace by  $\text{expression} \cdot (\text{row } r)$

## 1.24 Functions - neg

neg(expression) :

expression : real, vector, matrix, equation

result : real, vector, matrix, equation

Returns the negative of the expression.

---

## 1.25 Functions - rang

`rang(expression)` :

expression : matrix, equation

result : real, equation

Returns the rang of the matrix. This is the number of non-zero rows of `solve(expression)`.

## 1.26 Functions - sign

`sign(expression)` :

expression : real, equation

result : real, equation

Return 1 if expression is  $> 0$

Return 0 if expression is  $= 0$

Return -1 if expression is  $< 0$

## 1.27 Functions - solve

`solve(expression)` :

expression : matrix

result : matrix

Returns the solution of the matrix. This is the result of basic matrix transformations to convert the left square of the matrix into a standart matrix. This usually make only sense for non-square matrices.

## 1.28 Functions - spur

`spur(expression)` :

expression : matrix, equation

result : real, equation

Returns the spur of the matrix.

## 1.29 Functions - sqrt

`sqrt(expression)` :

expression : real, equation

result : real, equation

Returns the square root of the expression.

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### 1.30 Functions - swaprows

swaprows(matrix,r1,r2) :

matrix : matrix (must be variable or parameter)

r1 : real (should be integer)

r2 : real (should be integer)

result : matrix

This will copy the input matrix, except that row r1 and row r2 are swapped.

### 1.31 Functions - taylor

taylor(function,a,grade) :

This will calculate a taylor approximation for the given function of one variable at a of the given grade. If you omit the grade, a default of 2 will be used.

There are different kinds of syntax for this command :

1) Taylor approximation for an already defined function of one variable :

taylor(functionname, a, grade) - e.g.

f(x)=sin(x)

taylor( f, 0, 2 )

2) Taylor approximation for an explicit given function of one variables :

taylor( (expression)(var), a, grade) - e.g.

taylor( (sin(x))(x) , 0, 2)

### 1.32 Functions - trans

trans(expression) :

expression : matrix, equation

result : matrix, equation

Returns the transposition of the matrix.

### 1.33 Functions - umatrix

umatrix(size) :

result : matrix

This will create a standard matrix of the given size.

### 1.34 Functions - vector

`vector(list) :`

This will create a vector object. list is a list of expressions separated by commas. The components must evaluate to real. E.g.

`vector(1,2,3)`

`/1\`

`|2|`

`\3/`

### 1.35 Functions - window

`window(name) :`

This will open a window, displaying the named object.